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Four Colors and Associativity

Abstract for the Combinatorics Seminar 2011 October 4

The Four-Color Theorem was first proved by Appel and Haken in 1977 with the aid of a computer. Later, a second proof was given by Robertson, Sanders, Seymour, and Thomas. While the proof was simplified, it still relies on a computer in a significant way.

In 1990, Kauffman proved that the Four-Color Theorem is equivalent to the ability to find a non-trivial assignment of the 3-dimensional unit vectors \mathbf{i} , \mathbf{j} , and \mathbf{k} to the variables of two associations of the multiple cross product $\mathbf{v}_1 \times \mathbf{v}_2 \times \cdots \times \mathbf{v}_n$, such that both associations have the same evaluation. (An assignment is *trivial* if it evaluates to zero.) The associations are determined by the map being colored.

Since elements of Thompson's group F represent instances of the associative law, one can prove that the Four-Color Theorem is equivalent to every element of F 's having a non-trivial assignment of the vectors \mathbf{i} , \mathbf{j} , and \mathbf{k} for which that element's instance of associativity holds. I will prove that every positive element of F has such an assignment.

We call such elements *colorable*. I will consider several operations that preserve colorability of elements of F .

From:

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Last update: **2020/01/29 19:03**

