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### Rational Generating Functions and Compositions of an Integer

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#### Abstract for the Colloquium 2006 March 24

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A *composition* of the nonnegative integer  $n$  is a way of writing  $n$  as an ordered sum of positive integers. So, the compositions of 3 are  $1+1+1$ ,  $1+2$ ,  $2+1$ , and 3 itself. It is well known (and easy to prove) that if  $c_n$  is the number of compositions of  $n$  then  $c_n = 2^{n-1}$  for  $n$  at least 1, and  $c_0 = 1$ . Equivalently, we have the generating function

$$\sum_{n \geq 0} c_n x^n = (1-x)/(1-2x),$$

which is a rational function. We show that this is a special case of a more general family of rational functions associated with compositions. Our techniques include the use of formal languages. Surprisingly, identities from the theory of hypergeometric series are needed to do some of the computations.

This is joint work with Anders Björner.

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