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On Sperner's Inequality and Its Generalizations

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Sperner's inequality concerns the set $P(S)$ consisting of all subsets of a finite set S , partially ordered by subset inclusion. A *chain* is a linearly ordered subset of $P(S)$. In 1928, Sperner found a bound (in terms of the size of S) for the size of an antichain, that is, a subset of $P(S)$ in which there are no nontrivial chains. His result was generalized in two different directions: About 25 years later, Erdős extended Sperner's inequality to r -systems, that is, subsets of $P(S)$ in which chains contain at most r elements. Roughly another 25 years later, Meshalkin proved a Sperner-like inequality for a certain family of compositions (ordered partitions) of S . It's been about 25 years since Meshalkin's theorem, and hence about time for another extension. Xueqin Wang and I unify Erdős's and Meshalkin's inequalities and generalize them to a less restrictive family of compositions of S . As with the known theorems, our result has analogues in the poset of subspaces of a vector space.

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