Discrete Maths Section 1 (Spring 2020)

This is the official website of math314-01-s20.11 Please read our syllabus...

Due to the COVID-19 pandemic, our course has gone entirely online. Please carefully read the updated syllabus and the site below.

THIS PAGE NO LONGER RECEIVES UPDATES

General Information

Meetings: Meetings take place during our old class time (08:00 - 09:30 on MWF).

Office Hours: By appointment on Zoom. Appointments should be made for reasonable times of the day ("reasonable" as defined by me).

Textbook: Discrete Mathematics and its Applications (8e) by Kenneth Rosen.

Grading: See the course syllabus for a grade distribution.

Content: Propositional logic, methods of proof, naive set theory, functions and relations, induction and recursion, counting, and basic graph theory.

Content Delivery

Videos: I will upload videos to replace some lectures. You are to watch these videos, take notes, and answer any questions posed in them.²⁾

Notes: I will sometimes post PDFs for you to read. These are assigned reading; take notes on these PDFs, as they are fair game for homework and the final exam.

Readings: I will still assign reading from the textbook.

Problem Sessions: Roughly twice a week, I will host a problem session on Zoom during our old class meeting time. You are expected to attend these sessions.

Homework

Here is a quick look at what you will need to submit homework for the remainder of the course.

Submission

Homework is to be submitted as a PDF through Gradescope; the company has made their service free-to-use for this semester. See the Gradescope guide for students and watch the Gradescope video on submitting homework.

I will not accept homework in any form other than PDF.

I will not accept homework via email. Use Gradescope.

Miscellany

I offer you 1 homework bonus point per homework turned in using the LaTeX typesetting language; you must typeset exercises legibly. I wrote a short PDF on how to use LaTeX; you can use its source code as a startup template. The easiest way to get started is to make an account on Overleaf so you can view and compile .tex files; if you end up using LaTeX more frequently, you will probably want a different setup.

If you choose not to learn LaTeX, you can use a PDF scanning application to submit your homework. I think "Tiny Scanner" is nice; you can download it on your phone with either Android or iOS.

Here are documents on basic proof techniques and proof-writing style for your reference.

Participation

As a portion of your grade, you must contribute to our class notes. This can be done in one of the following two ways.

- **Notes**: Typing a portion of our notes from lectures (either one or two lectures).
- **Project**: Typing a short report on some topic related to our course.

All contributions must be approved by me in advance. The typing can be done either as plain-text or in \$\LaTeX{}\$; in either case students must discuss formatting with me before beginning their work.

Schedule

22 January 2020 W

- Review Syllabus
- Basic Logic and Sets
 - Propositions
 - Logical Connectives
- Homework:
 - Read textbook sections 1.1, 1.3.1 1.3.5

24 January 2020 F

- Basic Logic and Sets
 - Translation of Sentences
 - Logical Equivalence
- Homework:
 - Read textbook sections 1.4 1.5

27 January 2020 M

- Basic Logic and Sets
 - Predicates and Quantifiers
- Homework:
 - Read textbook sections 2.1 2.2 and 1.6

29 January 2020 W

- Basic Logic and Sets
 - Sets and Set Operations
 - Rules of Inference
- Homework:
 - Read textbook section 1.6
 - Think about the relationship between the logic we know and the basic operations of set theory.

31 January 2020 F

- Basic Logic and Sets
 - Natural Deduction
- Homework:
 - Complete these exercises (Due: 10 February 2020)
 - Enjoy the Superb Owl! (more information here if you're unfamiliar)

3 February 2020 M

- Elementary Properties of Divisibility
 - Some careful mathematical proofs
- Homework:
 - Read textbook section 4.3; pay special attention to sections 4.3.2, 4.3.4, and 4.3.7-4.3.8.
 - Attempt problems from the textbook.
- Add\Drop Deadline is TODAY!

5 February 2020 W

- Modular Arithmetic
 - Constructed \$\mathbb{Z}/n\mathbb{Z}\$\$
 - Studied more basic properties of divisibility
- Homework:
 - Read textbook section 4.4; pay special attention to sections 4.4.2 and 4.4.5.
 - Attempt problems from the textbook.

7 February 2020 F

- sNOw Classes
 - Homework is still due on Monday.

• Also still do the reading for Monday.

10 February 2020 M

- Greatest Common Divisor
 - Euclid's Algorithm
- Modular Arithmetic
 - Units in \$\mathbb{Z}\/n\mathbb{Z}\$\$
 - Solving Equations in \$\mathbb{Z}\/n\mathbb{Z}\$\$

Homework:

- Collected Homework 1
- **Due Wednesday**: Prove the following proposition.
 - Let \$a \in \mathbb{Z}\$ and \$m \in \mathbb{Z}^+\$. Integer \$a\$ is a unit modulo \$m\$ if and only if \$\gcd(a, m) = 1\$.
- Attempt problems from the textbook.

12 February 2020 W

- Primes and Factorization
 - Prime numbers and prime sieves
 - Fundamental Theorem of Arithmetic

Homework:

- Read textbook section 4.6
- Watch this video from KhanAcademy.org.
- Attempt problems from the textbook.

14 February 2020 F

- Application:
 - RSA Cryptography
 - RSA Problems

Homework:

- Read textbook section 5.1.
- Attempt problems from the textbook.

17 February 2020 M

- Mathematical Induction
 - Introduction (with dominoes!)
 - Many simple examples

Homework:

• Attempt problems from the textbook.

19 February 2020 W

Mathematical Induction

- Fibonacci Numbers
- More proofs by induction

Homework:

Attempt problems from the textbook.

21 February 2020 F

- Review Session for Exam 1
 - Student questions only
- Homework: Study!!!

24 February 2020 M

Midterm Exam 1 (In Class)

26 February 2020 W

- Mathematical Induction
 - Review of Weak Induction
 - Strong Induction

Homework:

- Read textbook section 5.2
- Watch this video on strong induction examples.
- Attempt problems from the textbook.

28 February 2020 F

- Mathematical Induction
 - More Strong Induction
 - The Well Ordering Principle

Homework:

- **Due Monday**: Find (with proof!) all integers of the form n = 5s + 9t for some $s, t \in \mathbb{N}$.
- Read textbook section 5.3
- Watch this video on comparing weak induction, strong induction, and well ordering (you can stop watching around the 5:45 marker).
- Attempt problems from the textbook.

2 March 2020 M

- Recursion
 - Some interesting relationships among on Fibonacci numbers
 - NB: Recursion is an extremely important concept; much of what we do in the rest of the course requires understanding this fundamental topic...

Homework:

- **Due Wednesday**: Prove that every Fibonacci number with odd index (i.e. \$f_{2k+1}\$ for \$k \in \mathbb{N}\$) can be expressed as a sum of squares of Fibonacci numbers.
- Read textbook section 6.1

• Attempt problems from the textbook.

4 March 2020 W

- Enumeration
 - Cardinality of Sets
 - Basic Counting Techniques
 - Product Principle: If \$A\$ and \$B\$ are finite sets, then \$\#(A \times B) = \#A \cdot \#B\$.
 - Sum Principle: If A and B are disjoint finite sets, then $A \subset B$ = A + B.
 - NB: Take note that \$A\$ and \$B\$ must be disjoint!
 - Correspondence Principle: Let \$A\$ and \$B\$ be finite sets. If there is a rule of assignment \$R \subseteq A \times B\$ such that both \$A = \{a : (a, b) \in R \text{ for some } b \in B\}\$ and \$\#\{b : (a, b) \in R\} = 1\$ for all \$a \in A\$, and \$B = \{b : (a, b) \in R \text{ for some } a \in A\}\$ and \$\#\{a : (a, b) \in R\} = 1\$ for all \$b \in B\$, then \$\#A = \#B\$.
 - Many Examples

Homework:

- Read textbook sections 6.3 and 6.4
- Attempt problems from the textbook.

6 March 2020 F

No Class (Winter Break)

9 March 2020 M

- Enumeration
 - Binomial Coefficients
 - Proved several identities via counting
 - Binomial Theorem: Let $n \in \mathbb{N}$. For all $x, y \in \mathbb{R}$ we have $(x + y)^n = \sum_{k=0}^n \dim_n^{k} x^k y^{n-k}$.

Homework:

- Read section 8.5 (NB: Yes, I mean "8.5"; it is not a typo)
- **Due Wednesday** Give two proofs that for all $n \in \mathbb{Z}^+$ we have $\sum_{k=0}^n (-1)^k \\ 0$, where k=0, and k=0, and
 - Use the Binomial Theorem.
 - Use a direct counting argument (*Hint*: move the negative terms to the other side before you start counting).
- Attempt problems from the textbook.

11 March 2020 W

- Enumeration
 - Inclusion-Exclusion Principle: For all finite sets \$A\$ and \$B\$ we have \$\#(A \cup B) = \#A + \#B \#(A \cap B)\$.
 - NB: Compare this with the Sum Principle...

Homework:

Attempt problems from the textbook.

13 March 2020 F

- Enumeration
 - NB: This lecture taught over Zoom.
 - Problem session on enumeration.

Homework:

Attempt problems from the textbook.

Note on Coronavirus Changes

In response to the COVID-19 pandemic, the remainder of the course went online. I have grouped the remainder of the semester by week (because this is more natural for an online course).

Old Lecture Notes

Here are lecture notes taken and plain-text typed by students-with editing and further LaTeX formatting done by me-for lectures before the class went online.

- Lecture Notes: Divisibility.
- Lecture Notes: Modular Arithmetic.
- Lecture Notes: Weak Induction.
- Lecture Notes: Strong Induction.
- Lecture Notes: Primes and Factorization.
- Lecture Notes: Fibonacci Numbers.
- Lecture Notes: Counting Techniques.
- Lecture Notes: Binomial Coefficients.

Week 9 (15 March 2020 -- 22 March 2020)

- Topics: Enumeration
 - Pigeonhole Principle and Generalized Pigeonhole Principle
 - Textbook section 6.2.
 - Lecture notes on the Pigeonhole Principle.
 - Video on the Generalized Pigeonhole Principle.
 - Lecture notes on the Generalized Pigeonhole Principle.
 - Anagrams
 - Textbook section 6.5.
 - Lecture notes.
 - Video on counting anagrams.
 - Counting Poker Hands (for practice; this is a different kind of counting cards...).

Homework:

- Submit a PDF to Gradescope with the text "This is a test homework. I took this opportunity to familiarize myself with Gradescope and making PDF submissions." (Due 23 March 2020)
 - See the <u>homework section</u> for more information.
- Complete these counting problems (Due 27 March 2020).

Week 10 (22 March 2020 -- 28 March 2020)

- Topics: Functions and Relations.
 - Introduction to Relations
 - Textbook sections 9.1 and 9.3.
 - Lecture notes.
 - Video on relations: reflexive, symmetric, and transitive (PS. this guy's videos are pretty great!).
 - Equivalence Relations and Closures
 - Textbook sections 9.5 and 9.4.
 - Lecture notes.
 - Video on equivalence relations (this YouTube channel is also pretty nice!).
 - Functions
 - Textbook section 2.3.
 - Notes on functions and relations.
 - Video on injective functions.
 - Video on surjective functions.

Homework:

Complete these homework problems (Due 13 April 2020).

Week 11 (29 March 2020 -- 4 April 2020)

- **Topics**: Graph Theory.
 - Introduction to Graphs
 - Textbook sections 10.1 10.3 (just for reference, see the lecture first).
 - Lecture Notes: Introduction to Graphs.
 - Lecture Notes: Proof of the Handshake Lemma.
 - Lecture Notes: Subgraphs and Counting Subgraphs of \$K n\$.
 - Connection in Graphs
 - Textbook section 10.4.
 - Lecture Notes: Graph Connection.

Spring Break (5 April 2020 -- 11 April 2020)

No Scheduled Meetings.

Week 12 (12 April 2020 -- 18 April 2020)

- Topics: Graph Theory
 - Eulerian and Hamiltonian Graphs
 - Textbook section 10.5.
 - Lecture Notes on Eulerian and Hamiltonian Graphs.
 - Graph Coloring
 - Textbook section 10.8.
 - Lecture Notes on Graph Coloring.

Week 13 (19 April 2020 -- 25 April 2020)

- Topics: Trees
 - Characterizing Trees
 - Textbook section 11.1.
 - Lecture Notes: Characterizing Trees.
 - Spanning Trees
 - Textbook sections 11.4 and 11.5.
 - Lecture Notes: Spanning Trees.
 - Storing Labeled Trees
 - Lecture Notes: Pruefer Code.
- Homework:
 - Complete these graph theory problems (Due 8 May 2020).
 - Optional: Implement the Pruefer code algorithm and its inverse in your favorite programming language.

Week 14 (26 April 2020 -- 2 May 2020)

- **Topics**: Models of Computation
 - Finite State Machines
 - Textbook section 13.2.
 - Lecture Notes.
 - Deterministic Finite State Automata
 - Textbook section 13.3.
 - Lecture Notes.
 - Noneterministic Finite State Automata
 - Textbook section 13.4.
 - Lecture Notes.

Week 15 (3 May 2020 -- 9 May 2020)

Review for Final.

FINAL EXAM

Due to the COVID-19 pandemic, final exams will be administered orally over Zoom.

Here a list of topics to guide your studying for your oral final.

¹⁾ If you have an idea to improve this space, please email eppolito-at-math-dot-binghamton-dot-edu with your suggestion; I would like this space to be as useful to students as possible...

²⁾ If you have trouble viewing the videos through Safari, you can either use another browser or try this solution from reddit.

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