

TeX code compiled with `\documentclass{beamer}` using the Amsterdam theme. There is one png image needed to compile slides:

`arc_chord_limit.png`

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\begin{document} \begin{frame} \large \begin{block} {} \begin{center} \$\displaystyle\lim_{x\rightarrow 0}\frac{\sin(x)}{x} = 1 \hspace{15pt} \displaystyle\lim_{x\rightarrow 0}\frac{\cos(x)-1}{x} = 0\$ \end{center} \end{block} Evaluate the limits: \vskip 5pt \begin{columns} \begin{column}{0.5\textwidth} \$\$ \lim_{x\rightarrow 0}\frac{\sin(6x)}{\sin(9x)}\$ \$ \vskip 15pt \$\$ \lim_{\theta\rightarrow 0}\frac{\cos(7\theta)-1}{\sin(9\theta)}\$ \$ \vskip 15pt \$\$ \lim_{t\rightarrow 0}\frac{\tan(16t)}{\sin(4t)}\$ \$ \end{column} \begin{column}{0.5\textwidth} \$\$ \lim_{x\rightarrow 0}\frac{x^2+6x-16}{x^2}\$ \$ \vskip 15pt \$\$ \lim_{x\rightarrow 2}\frac{\sin(x)-\cos(x)}{x-2}\$ \$ \end{column} \end{columns} \end{frame} \begin{frame} \LARGE Use both the derivatives of  $\sin(x)$  and  $\cos(x)$  and the quotient rule to show: \\ \$\$ \frac{d}{dx}(\tan(x)) = \sec^2(x) \$\$ and \\ \$\$ \frac{d}{dx}(\sec(x)) = \sec(x)\tan(x) \$\$ \end{frame} \begin{frame} \LARGE \begin{columns} \begin{column}{0.5\textwidth} Find  $f'(x)$ : \\ \$\$ f(x) = 5x^2 + 7\sin(x) \$\$ \vskip 20pt Find  $g'(\theta)$ : \\ \$\$ g(\theta) = \sec(\theta)\tan(\theta) \$\$ \end{column} \begin{column}{0.5\textwidth} Find  $F'(x)$ : \\ \$\$ F(x) = \frac{3 - \sec(x)}{\tan(x)} \$\$ \vskip 20pt Evaluate: \\ \$\$ \frac{d^2}{d\theta^2}(\sec(\theta)\tan(\theta)) = \sec^2(\theta)\tan(\theta) + \sec(\theta)\sec^2(\theta) \$\$ \end{column} \end{columns} \end{frame} \begin{frame} \LARGE Find the equation of the tangent line to the curve  $y = 14x\sin(x)$  at  $x = \pi/2$ . \vskip 55pt Find \\ \$\$ \frac{d^{103}}{dx^{103}}(\sin(x)) = \frac{d^{201}}{dx^{201}}(\cos(x)) \$\$ \end{frame} \begin{frame} \emph{Step into your teacher's shoes. What is wrong (if anything) with the following calculations? Explain any errors and correct for them.} \vskip 5pt \begin{block} {} Find all values of  $x$  in the interval  $[0, 4\pi]$  that satisfy the equation  $\sin(2x) = \cos(x)$ . \bf{Solution:} Since  $\sin(2x) = 2\sin(x)\cos(x)$ ,  $\sin(2x) = \cos(x)$  \vskip 20pt \Rightarrow \hspace{20pt} \begin{aligned} & \sin(x) = 1 \\ & \sin(x) = \frac{1}{2} \end{aligned} Therefore,  $x = \frac{\pi}{3}$  or  $x = \frac{5\pi}{3}$ . \end{block} \end{frame} \begin{frame} What does  $\lim_{x\rightarrow 0}\frac{\sin(x)}{x} = 1$  mean? Explain why three of the options are false and one is true. \begin{itemize} \item[a]  $\frac{0}{0} = 1$  \item[b] The tangent to the graph of  $y = \sin(x)$  at  $(0, 0)$  is the line  $y = x$ . \item[c] You can cancel the  $x$ 's. \item[d]  $\sin(x) = x$  for  $x$  near 0. \end{itemize} \end{frame} \begin{frame} The figure shows a circular arc of length  $s$  and a chord of length  $d$ , both subtended by a central angle  $\theta$ . Find  $\lim_{\theta\rightarrow 0^+}\frac{s}{d}$ . \begin{center} \includegraphics[height=2in]{arc_chord_limit.png} \end{center} It may be helpful to review the formulas associated to arcs and isosceles triangles. Further, why would the limit  $\lim_{\theta\rightarrow 0}\frac{s}{d}$  not exist? \end{frame} \end{document}
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From:

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