

TeX code compiled with `\documentclass{beamer}` using the Amsterdam theme.

`\begin{document} \begin{frame} \LARGE` Find two numbers whose difference is \$140 and whose product is a minimum. `\vspace{\stretch{1}}` Find the dimensions of a rectangle with perimeter \$60 meters whose area is as large as possible. `\end{frame} \begin{frame}` Consider the following problem: A box with an open top is to be constructed from a square piece of cardboard, \$3 feet wide, by cutting out a square from each of the four corners and bending up the sides. Find the largest volume that such a box can have. `\begin{enumerate}[a]` \item Draw several diagrams to illustrate the situation, some short boxes with large bases and some tall boxes with small bases. Find the volumes of several such boxes. `\vskip 15pt` \item Draw a diagram illustrating the general situation. Let  $x$  denote the length of the side of the square being cut out. Let  $y$  denote the length of the base. `\vskip 15pt` \item Write an expression for the volume  $V$  in terms of  $x$  and  $y$ . `\vskip 15pt` \item Use the given information to write an equation that relates the variables  $x$  and  $y$ . `\vskip 15pt` \item Use part (d) to write the volume as a function of  $x$ . `\vskip 15pt` \item Finish solving the problem by finding the largest volume that such a box can have. `\end{enumerate} \end{frame} \begin{frame} \LARGE` A rectangular storage container with an open top is to have a volume of \$10 cubic meters. The length of this base is twice the width. Material for the base costs \$5 per square meter. Material for the sides costs \$3 per square meter. Find the cost of materials for the cheapest such container. `\ (Round your answer to the nearest cent.) \end{frame} \begin{frame} \Large` A manufacturer has been selling \$1000 flat-screen TVs a week at \$350 each. A market survey indicates that for each \$10 rebate offered to the buyer, the number of TVs sold will increase by \$100 per week. `\begin{enumerate}[a]` \item Find the demand function (price  $p$  as a function of units sold  $x$ ). \item How large a rebate should the company offer the buyer in order to maximize its revenue? \item If its weekly cost function is  $C(x) = 60,000 + 120x$  how should the manufacturer set the size of the rebate in order to maximize its profit? `\end{enumerate} \end{frame} \begin{frame} \LARGE` A boat leaves a dock at 1 PM and travels due south at a speed of 20 km/h. Another boat has been heading due east at 15 km/h and reaches the same dock at 2 PM. How many minutes after 1 PM were the two boats closest together? `\end{frame} \begin{frame} \LARGE` At which points on the curve  $y = 1 + 40x^3 - 3x^5$  does the tangent line have the largest slope? `\end{frame} \begin{frame} \LARGE` A piece of wire 30m long is cut into two pieces. One piece is bent into a square and the other is bent into an equilateral triangle. `\vskip 5pt \begin{enumerate}[a]` \item How much wire should be used for the square in order to maximize the total area? `\vskip 15pt` \item How much wire should be used for the square in order to minimize the total area? `\end{enumerate} \end{frame} \begin{frame} \LARGE` A Norman window has the shape of a rectangle surmounted by a semicircle. (Thus the diameter  $x$  of the semicircle is equal to the width of the rectangle.) If the perimeter of the window is 32 ft, find the value of  $x$  so that the greatest possible amount of light is admitted. `\vspace{\stretch{1}} \end{frame} \begin{frame}` A designer wants to introduce a new line of bookcases. He wants to make at least 100 bookcases, but not more than \$2000 of them. He predicts the cost of producing  $x$  bookcases is  $C(x)$ . Assume that  $C(x)$  is a differentiable function. Which of the following must he do to find the minimum average cost,  $c(x) = \frac{C(x)}{x}$ ? `\begin{enumerate}` \item [bf I] find the points where  $c'(x) = 0$  and evaluate  $c(x)$  there \item [bf II] compute  $c''(x)$  to check which of the critical points in (I) are local maxima. \item [bf III] check the values of  $c$  at the endpoints of its domain. `\end{enumerate} \begin{enumerate}` \item I only \item I and II only \item I and III only \item I, II and III `\end{enumerate} \end{frame} \begin{frame}` The rate (in appropriate units) at which photosynthesis takes place for a species of phytoplankton is modeled by the function  $P = \frac{120I}{I^2 + I + 4}$  where  $I$  is the light intensity (measured in thousands of foot-candles). For what light intensity is  $P$  a maximum? `\end{frame} \begin{frame}` What is the maximum vertical distance between the line  $y = x + 6$  and the parabola  $y = x^2$  for  $-2 \leq x \leq 3$ ? `\end{frame} \begin{frame}` Find the area of the largest rectangle that can be inscribed in the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  `\vspace{\stretch{1}} \end{frame} \begin{frame}` An oil refinery is located 1 km north of the north bank of a straight river that is 1 km wide. A pipeline is to be constructed from the refinery to storage tanks located on the south bank of the river 6 km east of the refinery. The cost of laying pipe is \$400,000 km over land to a point  $P$  on the north bank and \$800,000 km under the river to the tanks. To minimize the cost of the pipeline, how far downriver from the refinery should the point  $P$  be located? `\end{frame} \end{document}`

From:  
<http://www2.math.binghamton.edu/> - **Binghamton University Department of Mathematical Sciences**

Permanent link:  
**[http://www2.math.binghamton.edu/p/calculus/resources/calculus\\_flipped\\_resources/applications/3.7\\_optimization\\_tex](http://www2.math.binghamton.edu/p/calculus/resources/calculus_flipped_resources/applications/3.7_optimization_tex)**

Last update: **2015/08/29 03:19**

