

- $X$  has the normal distribution with mean  $\mu$  and standard deviation  $\sigma > 0$  if the probability density function of  $X$  is

$$f_X(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2}$$

for all  $x$ .

- $X$  has the gamma distribution with parameters  $\alpha > 0, \beta > 0$  if the probability density function of  $X$  is

$$f_X(x) = \frac{x^{\alpha-1} e^{-x/\beta}}{\beta^\alpha \Gamma(\alpha)}$$

when  $x \geq 0$  and 0 otherwise.

- $X$  has the beta distribution with parameters  $\alpha > 0, \beta > 0$  if the probability density function of  $X$  is

$$f_X(x) = \frac{x^{\alpha-1} (1-x)^{\beta-1}}{B(\alpha, \beta)}$$

when  $0 \leq x \leq 1$  and 0 otherwise.

$$B(\alpha, \beta) = \frac{\Gamma(\alpha)\Gamma(\beta)}{\Gamma(\alpha + \beta)}$$

- $X$  has the Poisson distribution with parameter  $\lambda$  if the probability mass function of  $X$  is

$$p_X(k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

when  $k = 0, 1, 2, \dots$

- The moment generating function of a Uniform random variable on the interval  $[a, b]$  is

$$\frac{e^{tb} - e^{ta}}{t(b-a)}$$

- The moment generating function of a Normal random variable with mean  $\mu$  and standard deviation  $\sigma > 0$  is

$$e^{\mu t + t^2 \sigma^2 / 2}$$

- The moment generating function of a gamma random variable with parameters  $\alpha > 0, \beta > 0$  is

$$(1 - \beta t)^{-\alpha}$$

- The moment generating function of a Binomial random variable with parameters  $n > 0, 0 \leq p \leq 1$  is

$$(pe^t - 1 - p)^n$$

- The moment generating function of a Geometric random variable with parameters  $0 \leq p \leq 1$  is

$$\frac{pe^t}{1 - (1-p)e^t}$$

- The moment generating function of a Poisson random variable with parameters  $0 \leq \lambda$  is

$$e^{\lambda(e^t - 1)}$$