

The calculus part is done. Now fill in the given of $\frac{dx}{dt} = 2$ when $x = 14$; thus

$$\frac{df}{dt} = \left[\frac{2}{5}(14) + 3 \right] [2] = \frac{43}{5} \cdot 2 = \frac{86}{5} = 17.2$$

That is, $\frac{df}{dt} = 17.2$ thousand dollars/summer

or the income from parking increases \$17,200 each summer.

But there's another question asked. It's how the rate is changing three summers from now.

Since $\frac{dx}{dt} = 2$ now (initial condition) then in three summers ^{the population x} ~~it~~ will be a new value of $(14)(3) = 42$ thousand tourists.

$$\text{Therefore, } \frac{df}{dt} = \left[\frac{2}{5} \underset{\substack{\uparrow \\ \text{new } x}}{(20)} + 3 \right] \left[\underset{\substack{\uparrow \\ \text{same } \frac{dx}{dt}}}{2} \right] = \$22,000$$

rate the meter income changes

How did we get the new x ?

We know $\frac{dx}{dt} = 2$ each summer (pop tourists increases 2000/summer)

In 3 summers, it's 6 higher than 14.

$$\text{So } x = 14 + 6 = 20 \text{ thousand tourists}$$