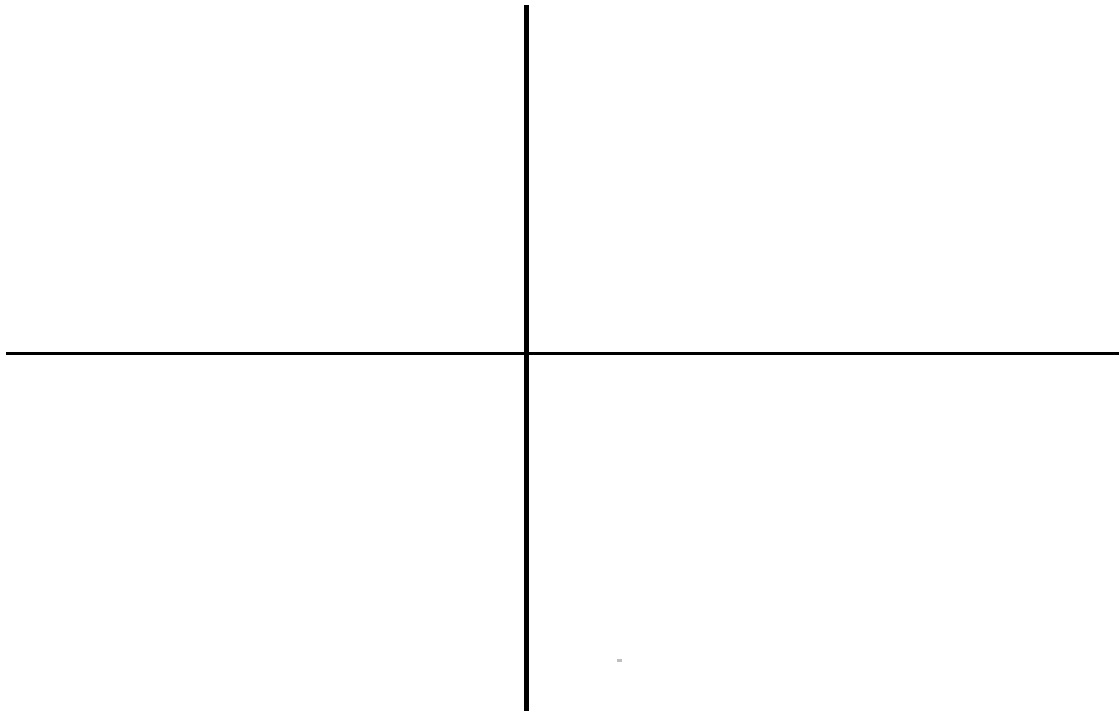


*Directions:* Answer each question as completely as possible. Show all work for credit. Good luck.

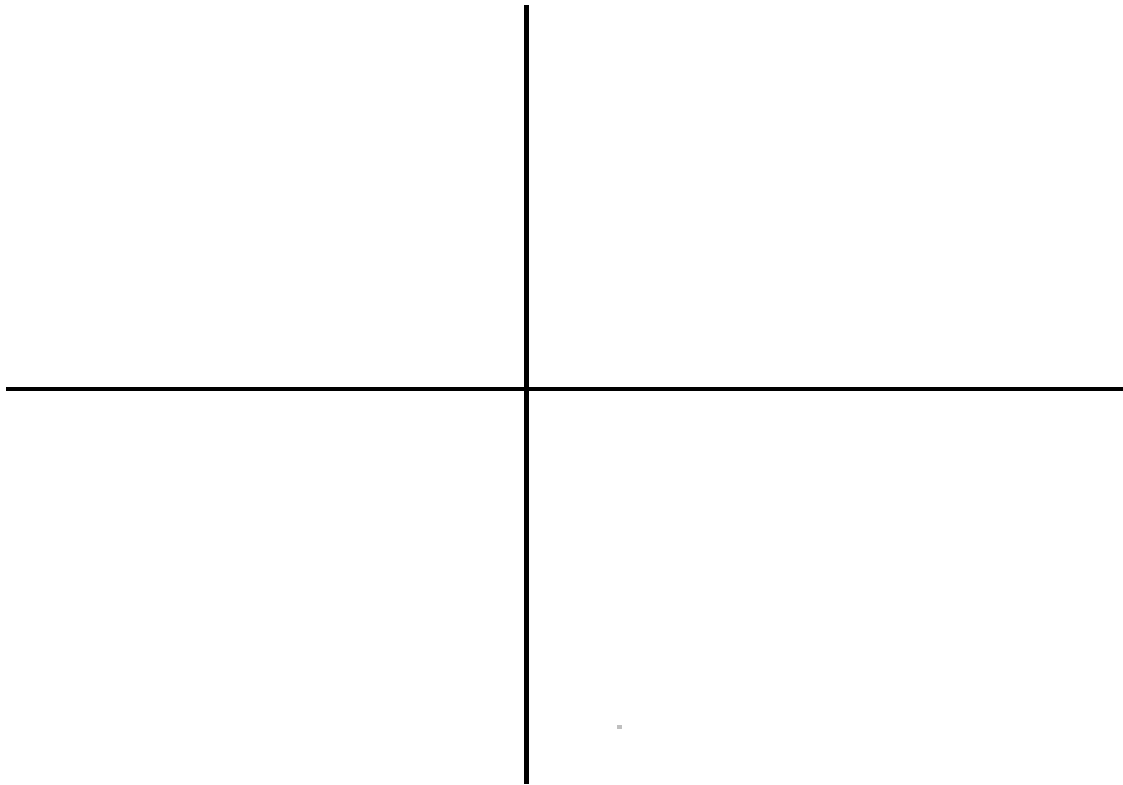
1. Suppose  $f(x) = \frac{(x^2 - 5x + 4)(x + 1)}{x^2 - 2x - 3}$

- a) Find the domain of  $f$ .
- b) Determine any “holes” in the graph of  $f$ , if any exist. If none exist, write NONE.
- c) Determine the equation of any vertical asymptotes to the graph of  $f$ .
- d) Determine the  $y$ -intercept of the graph of  $f$ .
- e) Determine any  $x$ -intercepts on the graph of  $f$ , if any exist.
- f) Find any other asymptotes (horizontal/slant) to the graph of  $f$ .
- g) Use the information found above to draw a rough sketch of the graph of  $f$ .



2. Suppose  $g(x) = \frac{-2x^3 + 12x^2 - 18x}{x^3 - 3x - 2}$

- a) Find the domain of  $g$ .
- b) Determine any “holes” in the graph of  $g$ , if any exist. If none exist, write NONE.
- c) Determine the equation of any vertical asymptotes to the graph of  $g$ .
- d) Determine the  $y$ -intercept of the graph of  $g$ .
- e) Determine any  $x$ -intercepts on the graph of  $g$ , if any exist.
- f) Find any other asymptotes (horizontal/slant) to the graph of  $g$ .
- g) Use the information found above to draw a rough sketch of the graph of  $g$ .



3. In each part, find the equation of a non-polynomial rational function  $f$  (in other words, the denominator should have a variable) having the following characteristics:

a) no vertical asymptotes and a slant asymptote

$$f(x) =$$

b) exactly one x-intercept, exactly two vertical asymptotes, and a horizontal asymptote of  $y = 2$ .

$$f(x) =$$