

Syllabus for Math 573 Applied Probability and Stochastic Processes

Books for Reference:

- N. C. van Kampen, Stochastic Processes in Physics and Chemistry.
- B. Oksendal, Stochastic Differential Equations, An Introduction with Applications

Topics:

1. General information about stochastic processes
  - A couple of examples: Gaussian Process, Poisson Process, Branching Process
  - Joint Distribution Functions
  - Kolmogorov's Extension Theorem
  - Correlations functions
2. Markov Processes
  - Kolmogorov's backward and forward equations
  - Chapman Kolmogorov's equations.
  - Master Equation
  - Semigroups and Generators
  - Markov Chains
3. Queuing and Renewal processes
4. Brownian Motion
  - Levy Construction
  - Properties of sample paths
5. Stochastic Integrals and Ito Formula
6. SDEs and Diffusions
  - Ito Formula
  - Kolmogorov's equations