

5-20 Evaluate the surface integral.

7. $\iint_S y \, dS$, S is the helicoid with vector equation $\mathbf{r}(u, v) = \langle u \cos v, u \sin v, v \rangle$,
 $0 \leq u \leq 1$, $0 \leq v \leq \pi$

13. $\iint_S x \, dS$, S is the surface $y = x^2 + 4z$, $0 \leq x \leq 1$, $0 \leq z \leq 1$

17. $\iint_S (x^2z + y^2z) \, dS$, S is the hemisphere $x^2 + y^2 + z^2 = 4$, $0 \leq z$

21-32 Evaluate the surface integral $\iint_S \mathbf{F} \cdot d\mathbf{S}$ for the given vector field \mathbf{F} and the oriented surface S . In other words, find the flux of \mathbf{F} across S . For closed surfaces, use the positive (outward) orientation.

23. $\mathbf{F}(x, y, z) = \langle xy, yz, zx \rangle$, S is the part of the paraboloid $z = 4 - x^2 - y^2$ that lies above the square $0 \leq x \leq 1$, $0 \leq y \leq 1$ and has upward orientation

27. $\mathbf{F}(x, y, z) = \langle 0, y, -z \rangle$, S consists of the paraboloid $y = x^2 + z^2$, $0 \leq y \leq 1$ and the disk $x^2 + z^2 \leq 1$, $y = 1$

31. $\mathbf{F}(x, y, z) = \langle x^2, y^2, z^2 \rangle$, S is the boundary of the solid half-cylinder $0 \leq z \leq \sqrt{1 - y^2}$, $0 \leq x \leq 2$