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### Topological Version of Pach's Overlap Theorem

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#### Abstract for the Combinatorics and Geometry/Topology Seminars 2018 May 1

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Consider the collection of all the simplices spanned by some  $n$ -point set in  $\mathbf{R}^d$ . There are several results showing that simplices defined in this way must overlap very much. In this talk I focus on the generalization of these results to 'curvy' simplices.

Specifically, Pach showed that every  $d+1$  sets of points,  $Q_1, \dots, Q_{d+1}$ , in  $\mathbf{R}^d$  contain linearly-sized subsets  $P_i$  in  $Q_i$  such that all the transversal simplices that they span intersect. In joint work with Alfredo Hubard, we show, by means of an example, that a topological extension of Pach's theorem does not hold with subsets of size  $C(\log n)^{1/(d-1)}$ . We show that this is tight in dimension 2, for all surfaces other than  $S^2$ . Surprisingly, the optimal bound for  $S^2$  is  $(\log n)^{1/2}$ . This improves upon results of Barany, Meshulam, Nevo, Tancer.

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