

Take-home trigonometry quiz—Due Monday April 24

Key

SHOW ALL YOUR WORK ON A SEPARATE PIECE OF PAPER.

You should be able to do this with no aids by now, notes or otherwise. The amount of looking things up you need to do is a good indication of how prepared you are for the test.

1. Fill in the information:

$y = \sin x$	dom: $x \in \mathbb{R}$	range: $[-1, 1]$	period: $2\pi$	amplitude: 1	roots on $[0, 2\pi]$ :
$y = \cos x$	dom: $x \in \mathbb{R}$	range: $[-1, 1]$	period: $2\pi$	amplitude: 1	roots on $[0, 2\pi]$ :
$y = \tan x$	dom: $x \neq \frac{n\pi}{2}$ , range: $\mathbb{R}$	period: $\pi$	amplitude: NA	roots on $[-\pi, \pi]$ :	$0, \pi, -\pi$

$$n = \pm 1, 3, 5, \dots \text{ or } n \text{ odd}$$

2. Fill in the information for each angle given:

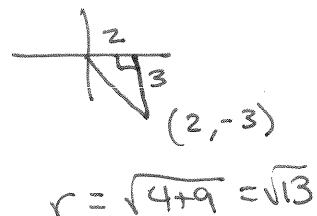
	Complement	Supplement	Positive coterminal	Negative coterminal
$64^\circ$	$26^\circ$	$116^\circ$	$424^\circ$	$-296^\circ$
$\frac{\pi}{12}$	$\frac{5\pi}{12}$	$\frac{11\pi}{12}$	$\frac{25\pi}{12}$	$-\frac{23\pi}{12}$

3. Fill in the information for each angle given:

	Conversion to $\pi$ 's or $^\circ$ 's	Quadrant	Reference angle (in given angle's units)
$-208^\circ$	$-\frac{52\pi}{45}$	II	$28^\circ$
$\frac{11\pi}{6}$	$330^\circ$	IV	$\frac{\pi}{6}$

4. The point  $(2, -3)$  lies on the terminal side of angle  $\theta$ . Find the six trigonometric values of  $\theta$ .

$$\begin{aligned} \sin \theta &= -\frac{3}{\sqrt{13}} & \csc \theta &= -\frac{\sqrt{13}}{3} \\ \cos \theta &= \frac{2}{\sqrt{13}} & \sec \theta &= \frac{\sqrt{13}}{2} \\ \tan \theta &= -\frac{3}{2} & \cot \theta &= -\frac{2}{3} \end{aligned}$$



$$r = \sqrt{4+9} = \sqrt{13}$$

Find the coordinates of the point on the *unit circle* that lies on the same terminal side of  $\theta$ .

$$\left( \frac{2}{\sqrt{13}}, -\frac{3}{\sqrt{13}} \right)$$

5. Evaluate each of these:

$$\sec(\pi) = \frac{1}{\cos\pi} = -1$$

$$\sin(5\pi) = 0$$

$$\tan(\pi/3) = \sqrt{3}$$

$$\cot(\pi/3) = \frac{1}{\sqrt{3}}$$

$$\cos(-\pi/2) = 0$$

$$\csc(0) = \text{ind}$$

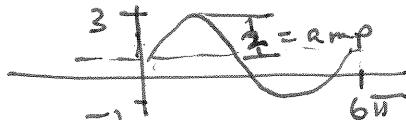
6. The sine function and the tangent function are odd functions. The cosine function is an even function.

$$\text{So, } \sin(-4\pi) = -\sin(4\pi) \quad \cos(-\pi/3) = \cos(\pi/3) \quad -\tan(5\pi/6) = \tan(-\frac{5\pi}{6})$$

7. What is the equation of a sine function that has an amplitude of  $\frac{1}{2}$ , a minimum value of  $-1$  and a maximum value of  $3$  (that is, a range of  $[-1, 3]$ , and a period of  $6\pi$ )?

$$\begin{aligned} \text{Per} &= 6\pi \\ \frac{2\pi}{B} &= 6\pi \\ B &= \frac{1}{3} \end{aligned}$$

$$y = \frac{1}{2} \sin\left(\frac{1}{3}x\right) + 1$$



8. Sketch two cycles of the graph of  $y = 5\cos(2\theta + \pi)$ . There is no vertical shift. It will help to first find:

$$\begin{aligned} \text{Amp} &= 5 & \text{Period} &= \frac{2\pi}{2} = \pi & \text{Horizontal shift} &= \frac{\pi}{2} \text{ left} & \text{Endpoints of one cycle} &= -\frac{\pi}{2}, \frac{\pi}{2} \end{aligned}$$

$$y = 5\cos 2(\theta + \frac{\pi}{2})$$

