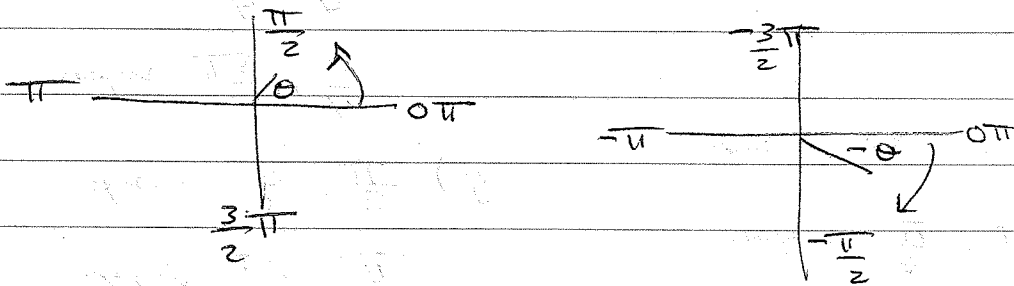
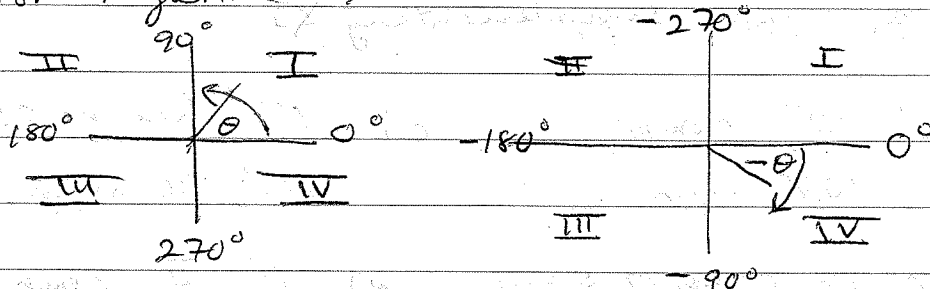
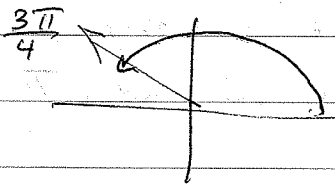


Ch. 8 HW - Trigonometry

#1 a) The quadrant is found by measuring, above the x -axis, counterclockwise (contre-montre in French) for positive θ , below the x -axis (clockwise) for negative θ .

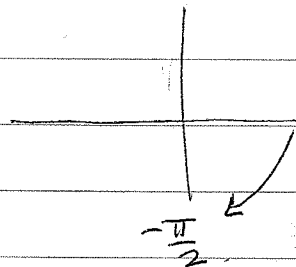


b) Coterminal angle measure is found by adding 2π or subtracting 2π from a given angle θ . You can also add or subtract multiples of 2π to arrive at a coterminal angle.



$$\frac{3\pi}{4} + 2\pi = \frac{11\pi}{4}$$

$$\frac{3\pi}{4} - 2\pi = \frac{-5\pi}{4}$$



$$-\frac{\pi}{2} + 3(2\pi) = \frac{11\pi}{2}$$

$$-\frac{\pi}{2} - 2\pi = \frac{-13\pi}{2}$$

#3) The complement of an angle θ is the angle, ^{whose} measure sums to 90 ($\pi/2$) with θ .

The supplement of an angle θ is the angle whose measure sums to 180 (π) with θ .

(a) $30^\circ, 60^\circ$ complementary \checkmark
 $30^\circ, 150^\circ$ supplementary \checkmark

(b) $78^\circ, 12^\circ$ comp. c) 110° has no complement
 $78^\circ, 102^\circ$ supp. $110^\circ, 70^\circ$ supp.

d) 270° no comp. or supp. e) $\frac{\pi}{4}, \frac{\pi}{4}$ comp

$\frac{\pi}{4}, \frac{3\pi}{4}$ supp

f) $\frac{5\pi}{6}$ no comp.

g) $\frac{\pi}{3}, \frac{\pi}{6}$ comp

$\frac{5\pi}{6}, \frac{\pi}{6}$ supp

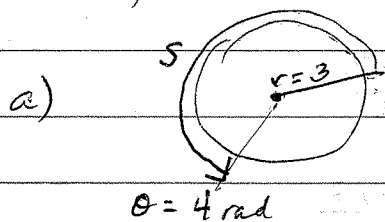
$\frac{\pi}{3}, \frac{2\pi}{3}$ supp

4) 1 rad — Recall that there are 2π rad in 360°
 so there are $\frac{2\pi}{4}$ or $\frac{\pi}{2} \approx \frac{3.14}{2}$ in 90°

(Here I'm checking that 1 rad is small enough to have a comp.)

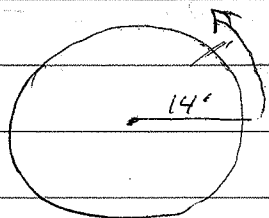
So, 1 rad, $\frac{\pi}{2} - 1$ comp, and 1 rad, $\pi - 1$ are supp

#5) Length of arc $s = r \cdot \theta$



$$s = 4 \cdot 3 = 12 \text{ cm}$$

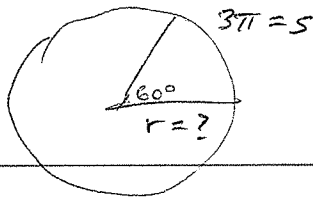
b)



$$s = r \cdot \theta$$

$$\theta = \frac{s}{r} = \frac{8}{14} = \frac{4}{7} \text{ rad}$$

#5 c)



You must change degree measure to radian measure to apply the formula. $60^\circ = \pi/3$ rad.

$$r = \frac{s}{\theta} = \frac{3\pi \text{ in}}{\pi/3} = 9 \text{ in}$$

#6)

Area of a sector = $\frac{1}{2}\theta r^2$ (θ in radian measure)

a) $A = \frac{1}{2} \cdot \left[\frac{\pi}{6}\right] \cdot r^2 = \left[\frac{\pi}{12} r^2\right]$ when $\left[\theta = 30^\circ\right]$

Notice that $30/360 = 1/12$ + Area of sector = $\frac{\text{Area of circle}}{12}$

b) $\theta = 147^\circ = \frac{147}{180}\pi \text{ rad} = \frac{49}{60}\pi$

$$A = \frac{1}{2}\theta r^2 = \frac{1}{2} \cdot \frac{49}{60} r^2 = \frac{49}{120} r^2$$

Again, notice that $147/360 = 49/120$

c) $\theta = 4 \text{ rad}$, $A = \frac{1}{2} \cdot 4 \cdot r^2 = 2r^2$

d) We're supposed to prove what we just used! That Area of sector = $\frac{1}{2}\theta r^2$. The ratios seen in (a)-(c) suggest the answer.

$$\frac{\text{sector } \theta}{\text{circle } 2\pi} = \frac{\theta}{2\pi} \quad \& \quad \frac{\text{area sector}}{\text{area circle}} = \frac{A_{\text{sec}}}{\pi r^2}$$

Setting angle ratios = area ratios in a proportion

gives $\frac{\theta}{2\pi} = \frac{A_{\text{sec}}}{\pi r^2}$ or $A_{\text{sec}} = \frac{\pi r^2 \theta}{2\pi}$
 $= \frac{r^2 \theta}{2}$ ✓

the first change in the price of the stock is

the second change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

the third change in the price of the stock is

the fourth change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

the fifth change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

the sixth change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

the seventh change in the price of the stock is

the eighth change in the price of the stock is

the ninth change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

the tenth change in the price of the stock is

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$

$$\Delta P = \frac{1}{2} \Delta P = \frac{1}{2} \Delta P$$