

$$f(0,2) = 0 - 2^2 = -4, \quad f(0,-2) = 0 - (-2)^2 = -4$$

So far, the two solns. give the same negative answer.

Go back to the partials, this time, F_y :

$$F_y = -2y(1-\lambda) = 0 \rightarrow \begin{array}{l} -2y = 0 \\ \boxed{y=0} \end{array} \text{ or } 1-\lambda = 0 \quad \lambda = 1$$

Substitute $y=0$ into the constraint:

$$x^2 + y^2 = 4 \rightarrow x^2 + 0^2 = 4 \rightarrow \boxed{x = \pm 2}$$

Test the two pts $(2,0)$ and $(-2,0)$ into $f(x,y)$ and compare to previous answers.

$$f(2,0) = 2^2 - 0 = 4, \quad f(-2,0) = (-2)^2 - 0 = 4$$

Hence, both $(2,0)$ and $(-2,0)$ give the maximum $f(x,y)$. And $(0,2)$ and $(0,-2)$ give the minimum.