HOFFMAN SEC 5.1 ANSWERS

CHAPTER 5 Section 1

1.
$$-3x + C$$

3.
$$\frac{x^6}{6} + C$$

5.
$$-\frac{1}{x} + C$$

7.
$$4\sqrt{t} + C$$

9.
$$\frac{5}{3}u^{3/5} + C$$

11.
$$t^3 - \frac{2\sqrt{5}}{3}t^{3/2} + 2t + C$$

13.
$$2y^{3/2} + y^{-2} + C$$

15.
$$\frac{e^x}{2} + \frac{2}{5}x^{5/2} + C$$

17.
$$\frac{u^{1.1}}{3.3} - \frac{u^{2.1}}{2.1} + C$$

$$-19. x + \ln x^2 - \frac{1}{x} + C$$

$$21. \quad -\frac{5}{4}x^4 + \frac{11}{3}x^3 - x^2 + C$$

23.
$$\frac{2}{7}t^{7/2} - \frac{2}{3}t^{3/2} + C$$

25.
$$\frac{1}{2}e^{2t} + 2e^t + t + C$$

27.
$$\frac{1}{3} \ln |y| - 10\sqrt{y} - 2e^{-y/2} + C$$

29.
$$\frac{2}{5}t^{5/2} - \frac{2}{3}t^{3/2} + 4t^{1/2} + C$$

$$31. \quad y = \frac{3}{2}x^2 - 2x - \frac{3}{2}$$

33.
$$y = \ln x^2 + \frac{1}{x} - 2$$

35.
$$f(x) = 2x^2 + x - 1$$

37.
$$f(x) = -\frac{1}{3}x^3 - \frac{1}{2}x^2 + \frac{31}{6}$$

39.
$$f(x) = \frac{x^4}{4} + \frac{2}{x} + 2x - \frac{5}{4}$$

41.
$$f(x) = -e^{-x} + \frac{x^3}{3} + 5$$

51. a.
$$18\frac{1}{3}$$
 (18 items)

b.
$$48\frac{1}{3}$$
 (48 items)

53. a.
$$T(t) = 16 - 20e^{-0.35t}$$

55. a.
$$P(q) = 100q - q^2 - 200$$

b.
$$q = 50$$
; \$2,300

57.
$$c(x) = 0.9x + 0.2x^{3/2} + 10$$

 The car travels 199.89 feet before stopping, so the camel gets nudged.

 a. f'(x) is maximized when x = 10; 7 items per minute

b.
$$f(x) = x + 0.6x^2 - 0.02x^3$$

c.
$$f'(20.8) = 0$$
; $f(20.8) \approx 100$ items

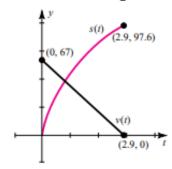
63.
$$v(r) = \frac{1}{2}a(R^2 - r^2)$$

65. 20 meters

67.
$$\int b^x dx = \int e^{x \ln b} dx = \frac{e^{x \ln b}}{\ln b} + C = \frac{b^x}{\ln b} + C$$

69. a.
$$v(t) = -23t + 67$$
; $s(t) = -\frac{23}{2}t^2 + 67t$

b.



c. v(t) = 0 when t = 2.9 sec and s(2.9) = 97.6 ft;

s(t) = 45 ft when $t \approx 0.77$ sec or 5.05 sec and

 $v(0.78) \approx 49.30$ ft/sec while $v(5.05) \approx -49.15$.

ANSWERS

CHAPTER 5 Section 2

1. a.
$$u = 3x + 4$$

b.
$$u = 3 - x$$

c.
$$u = 2 - t^2$$

d.
$$u = 2 + t^2$$

3.
$$\frac{1}{12}(2x+6)^6+C$$

5.
$$\frac{1}{6}(4x-1)^{3/2}+C$$

7.
$$-e^{1-x} + C$$

9.
$$\frac{1}{2}e^{x^2} + C$$

11.
$$\frac{1}{12}(t^2+1)^6+C$$

13. $\frac{4}{21}(x^3+1)^{7/4}+C$

15.
$$\frac{2}{5} \ln |y^5 + 1| + C$$

17.
$$\frac{1}{26}(x^2 + 2x + 5)^{13} + C$$

19.
$$\frac{3}{5} \ln |x^5 + 5x^4 + 10x + 12| + C$$

21. $-\frac{3}{2} \left(\frac{1}{u^2 - 2u + 6} \right) + C$

23.
$$\frac{1}{2}(\ln 5x)^2 + C$$

25.
$$\frac{-1}{\ln x} + C$$

27.
$$\frac{1}{2}[\ln{(x^2+1)}]^2 + C$$

29.
$$\ln |e^x - e^{-x}| + C$$

31.
$$\frac{1}{2}x - \frac{1}{4} \ln|2x + 1| + C$$

15/2 13/2

33. $\frac{1}{10}(2x+1)^{5/2} - \frac{1}{6}(2x+1)^{3/2} + C$

35.
$$2 \ln (\sqrt{x} + 1) + C$$

37.
$$y = -\frac{1}{6}(3 - 2x)^3 + \frac{9}{2}$$

39.
$$y = \ln|x+1| + 1$$

41.
$$y = \frac{1}{2} \ln |x^2 + 4x + 5| - \frac{1}{2} \ln 2 + 3$$

43.
$$f(x) = \frac{1}{5} - \frac{1}{5}(1 - 2x)^{5/2}$$

45.
$$f(x) = \frac{3}{2} - \frac{1}{2}e^{4-x^2}$$

47. a.
$$x(t) = -\frac{4}{9}(3t+1)^{3/2} + \frac{40}{9}$$

b.
$$x(4) = -16.4$$

c.
$$t = 0.4$$

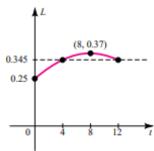
49. a.
$$x(t) = \sqrt{2t+1} - 1$$

b.
$$x(4) = 2$$

c.
$$t = \frac{15}{2}$$

51. a.
$$C(q) = (q - 4)^3 + 64 + k$$
, where k is the overhead

- 53. 2.3 meters
- **55. a.** $R(x) = 50x 175e^{-0.01x^2} + 175$
 - b. \$50,175
- **57. a.** $C(t) = \frac{1}{e^{0.01t} + 1}$
 - b. 0.3543 mg/cm³; 0.1419 mg/cm³
 - c. 294 minutes
- **59. a.** $L(t) = 0.03\sqrt{-t^2 + 16t + 36} + 0.07$; at t = 8 (3:00 p.m.); 0.37 parts per million
 - **b.** The ozone level at 11:00 A.M. (t = 4) is L(4) = 0.345. The same level occurs at t = 12 (7:00 P.M.).



- **61. a.** $p(x) = \frac{300}{\sqrt{x^2 + 9}} + 15$
 - **b.** \$66.45; \$115
 - c. 265
- 63. Profit declines by \$93,733.
- **65.** $\frac{3}{7}(x^{2/3}+1)^{7/2}-\frac{3}{5}(x^{2/3}+1)^{5/2}+C$
- 67. $e^x + 1 \ln(e^x + 1) + C$

CHAPTER 5 Section 3

- 1. 15
- 3. $\frac{95}{2}$
- 5. $\frac{6}{5}$
- 7. $-\frac{6}{5}$
- 9. $3 \frac{4}{e}$
- 11. 1.95
- **13.** 144

- 15. $\frac{8}{3} + \ln 3 \approx 3.7653$
- 17. $\frac{2}{9}$
- 19. 3.2
- 21. $\frac{4}{3}$
- 23. $\frac{7}{6}$
- 25. e
- 27. $\frac{8}{3}$
- **29.** $e^3 e^2$
- **31.** -20
- **33.** 0
- **35.** 5
- **37.** 3
- 39. $\frac{33}{5}$
- 41. $\frac{112}{9}$
- 43. 4
- **45.** $\frac{3}{2} \ln 3 \approx 1.6479$
- 47. V(5) V(0)
- **49.** \$480
- 51. 0.75 ppm
- 53. About 98 people

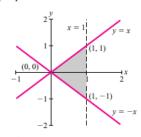
- **55.** \$75
- 57. $1,500\left(\frac{3}{2} + \frac{5}{4}\ln\frac{11}{9}\right) \approx 2,626$ telephone
- **59. a.** -\$48,036.33
 - b. \$28,546.52
- The concentration decreases by 0.8283 mg/cm³.
- 63. A decrease of \$1,870
- **65.** $2 \ln 2 \approx 1.386 \text{ grams}$
- **67.** $8\sqrt{11} 8\sqrt{6}$ or about 7 facts
- **69.** 96 ft
- 71. a. $\frac{\pi}{4}$
 - **b.** $\frac{\pi}{4}$; part of the area under the circle $(x-1)^2 + y^2 = 1$

ANSWERS

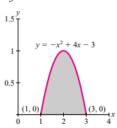
CHAPTER 5 Section 4

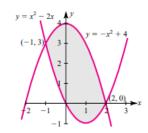
1.
$$\frac{5}{12}$$

3.
$$2 \ln 2 - \frac{1}{2}$$

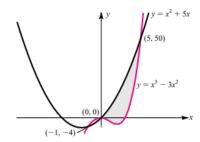


7. Area =
$$\frac{4}{3}$$





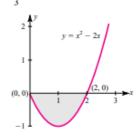
13. Area =
$$\frac{443}{6}$$

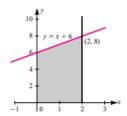




#15 continued below

9. Area =
$$\frac{4}{3}$$

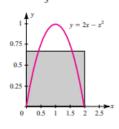




21.
$$\frac{3}{2}\left(e - \frac{1}{e}\right)$$

23.
$$\frac{\ln 5 - \ln}{\ln 3}$$

25. Average value =
$$\frac{2}{3}$$

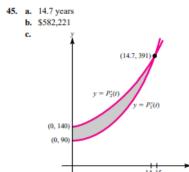


$$y = P_1(t)$$

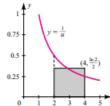
$$y = P_2(t)$$

$$(0, 306)$$

$$(16, 386)$$



27. Average value =
$$\frac{\ln 2}{2}$$



49.
$$\frac{1}{40}$$
 mg/cm³