## Homework 1 MATH 304 Section 3

$\begin{array}{ll}\text { Assigned: } & \text { Monday, September } 8 . \\ \text { Potentially Collected: } & \text { Monday, September } 15 .\end{array}$

1. Find the general solution of the system

$$
\begin{gathered}
x_{1}-2 x_{2}-x_{3}+3 x_{4}=0 \\
-2 x_{1}+4 x_{2}+5 x_{3}-5 x_{4}=3 \\
3 x_{1}-6 x_{2}-6 x_{3}+8 x_{4}=2
\end{gathered}
$$

2. Suppose that a $3 \times 5$ coefficient matrix for a system has three pivot columns. Is the system consistent? Why or why not?
3. Suppose that a system of linear equations has a $3 \times 5$ augmented matrix whose fifth column is a pivot column. Is the system consistent? Why or why not?
4. Suppose the coefficient matrix of a system of linear equations has a pivot position in every row. Explain why the system is consistent.
