

Final Review Quiz MATH 304 Section 3 Name:

Clearly circle "True" or "False" for each of the following problems. Circle "True" only if the statement is always true. No explanation necessary.

- TRUE FALSE (1) Given a subspace V of \mathbb{R}^n a vector $\vec{b} \notin V$, the projection $\vec{p} = \text{proj}_V(\vec{b})$ is the vector in V which makes $\|\vec{b} - \vec{p}\|$ minimal.
- TRUE FALSE (2) If S is a linearly dependent subset of the vector space V and $\vec{u} \notin \text{Span}(S)$, then $S \cup \{\vec{u}\}$ is linearly independent.
- TRUE FALSE (3) If V is a finite dimensional vector space, then any spanning set contains a basis for V .
- TRUE FALSE (4) If A is an 8×5 matrix of rank 5, then the linear transformation associated to A is one-to-one.
- TRUE FALSE (5) If A is a square matrix, then A is invertible. ← must have full rank
- TRUE FALSE (6) Suppose that V is a finite dimensional vector space with S a linearly independent subset of V and T a spanning set of V . Then S might contain more vectors than T .
- TRUE FALSE (7) The set of polynomials $\{ax^3 + b : a, b \in \mathbb{R}\}$ is a subspace of \mathbb{P}_3 . ← true if ≥ 4
- TRUE FALSE (8) There exists a subset X of \mathbb{R}^4 that spans \mathbb{R}^4 and that has three elements.
- TRUE FALSE (9) If U is a subspace of V and $F : V \rightarrow W$ is a ~~linear transformation~~, then $F(U)$ has the same dimension as U . ↑ true if isomorphism
- TRUE FALSE (10) Let $k > n$. The k dimensional vector space V can have a linearly independent set with n elements.
- TRUE FALSE (11) Every nonzero subspace of \mathbb{R}^n has an orthogonal basis. ← []
- TRUE FALSE (12) A square matrix always has eigenvalues and eigenvectors.
- TRUE FALSE (13) The dimension of an eigenspace must be nonzero.
- TRUE FALSE (14) For a subspace V of \mathbb{R}^n with basis X , the orthogonal complement V^\perp is computed using the column space of the matrix associated to X . ~~$\text{null}(X^T)$~~
- TRUE FALSE (15) If $F : V \rightarrow W$ and $G : W \rightarrow U$ are linear transformations whose composition, $GF : V \rightarrow U$ is 1-to-1 then G must be 1-to-1. ← $\mathcal{L} F$