

1. [10] 2. [15] 3. [10] 4. [10] 5. [15] 6. [10] 7. [10] 8. [10] 9. [10] Total: [100]

**Math 223**

**Midterm (8:00 AM version)**

**Sept 28, 2015**

*Name:*

*Section:*

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*Closed book and closed notes.*

*Answers must include supporting work.*

*Calculators and cell phones out of sight.*

1. (10 pts) Solve the following inequalities:

(a)  $|2 + 3x| \leq 3$

(b)  $|x - 1| > 3$

2. (15 pts)

(a) Determine  $f$  and  $g$  such that  $h(x) = f(g(x))$  for  $h(x) = \sqrt{4x - x^2}$ .

(b) Find the domain of  $h(x)$ .

3. (10 pts) Given a rectangle; its length is three times its width. Express its area  $A$  as a function of its perimeter  $P$ .

4. (10 pts) The equation  $2x^2 - 4x + 2y^2 + 8y + 1 = 0$  describes a circle. Determine the circle's center and radius by completing the square.

5. (15 pts) Sketch the following graphs:

(a)  $y = |x - 3| + 2$

(b)  $y = \sqrt{-x}$

(c)  $y = x^2 - 2x + 1$

6. (10 pts)

(a) Find a polynomial of degree 3 with zeros -3, 0, and 3.

(b) Is  $x - 1$  a factor of  $P(x) = x^7 + 4x^6 - 2x^5 + x^4 - x^2 + 2x - 5$ ? Explain your answer. [Hint: use the Factor Theorem]

7. (10 pts) Find the quotient and the remainder using long division.

$$\frac{3x^4 - 5x^3 - 20x - 5}{x^2 + x + 3}$$

8. (10 pts) Write the following polynomial in factored form.

$$P(x) = x^3 + 3x^2 - x - 3$$

9. (10 pts) Sketch the region bounded by the parabola  $x = y^2$  and the line  $y = x - 2$  and label their points of intersection.